Coding and Mathematical Definitions

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Definitions of R Code

R script: the lines of code and comments that you are writing (filename.R).

R project: your R script, any variables you have created, and your current R environment (filename.Rproj).

R package: a set of functions/code that you can load into your script (examples - dplyr, sp).

R Comment: does not run as code, starts with #. You use comments to explain what your code is doing in plain language.

Object or Variable: a unit of information that is stored in the workspace (computer memory) and can be recalled or manipulated. 'a' is an object. Specifically, a vector of length 3.

a = c(3, 2, 1)

Element: a piece of information within an object. The 1st element of a is...

a[<mark>1</mark>]

[1] 3

Function: a command to take inputs (objects or elements) and manipulates it to provide an output, which can be saved as a new object.

```
fun.text = function(x) {
    paste("Your input variable is ", x, sep = "")
}
```

fun.text(4)

[1] "Your input variable is 4"
fun.text("INPUT")

[1] "Your input variable is INPUT"

Argument: a specific command within a function. Many functional arguments are preset and do not need to be explitly stated.

x = c(1, 2, 3, NA)mean(x)

[1] NA

na.rm is an argument of the function mean to ignore the missing value. Its
preset is FALSE. If you have na's you need to change the argument to 'TRUE'.
mean(x, na.rm = TRUE)

[1] 2

Types of R Objects and Mathematical Notation

Vector: 1 row, many columns OR 1 column many rows. Can be numbers of characters.

v = c(4, 1, 3)
is.vector(v)

[1] TRUE

length(v)

[1] 3

Math notation (capitalized & lower case): \vec{v} or **v**

$$\mathbf{v} = \begin{bmatrix} 4 & 1 & 3 \end{bmatrix} \tag{1}$$

Matrix: Generalization of vectors. Can have 1 or more rows and columns. Only numbers.

M = matrix(1:10, nrow = 2)М ## [,1] [,2] [,3] [,4] [,5] ## [1,] 1 3 5 7 9 ## [2,] 2 4 6 8 10 dim(M)## [1] 2 5 is.vector(M) ## [1] FALSE is.matrix(M) ## [1] TRUE Math notation (capitalized & upper case): M

$$\mathbf{M} = \begin{bmatrix} 1 & 3 & 5 & 7 & 9 \\ 2 & 4 & 6 & 8 & 10 \end{bmatrix} \tag{2}$$

Array: Generalization of matrices. Can be n dimensional. Only numbers.

```
arr = array(1:100, dim = c(3, 4, 3))
arr
## , , 1
##
         [,1] [,2] [,3] [,4]
##
## [1,]
            1
                  4
                            10
                       7
## [2,]
            2
                  5
                       8
                            11
## [3,]
            3
                  6
                       9
                            12
##
##
   , , 2
##
##
         [,1] [,2] [,3] [,4]
## [1,]
           13
                16
                      19
                            22
                            23
## [2,]
           14
                 17
                      20
## [3,]
           15
                18
                      21
                            24
##
## , , 3
##
##
         [,1] [,2] [,3] [,4]
## [1,]
           25
                28
                      31
                            34
## [2,]
                29
                            35
           26
                      32
## [3,]
           27
                30
                      33
                            36
dim(arr)
## [1] 3 4 3
is.vector(arr)
## [1] FALSE
is.matrix(arr)
## [1] FALSE
is.array(arr)
## [1] TRUE
                                                                                  <sup>-</sup>34
                                                                  28
                                                         25
                                                                          31
                                                         26
                                                                  29,
                                                                          32
                                                                                  35
                                                                 30
                                                                          33
                                                                                  36
                              13
                                       16
                                                19
                                                        22
                                               20
                              14
                                       17.-
                                                        23
                                       18
                                               21
                                                        24
    1
             4
                     7
                             10
                                                        _ _ _ _
    \mathbf{2}
             5
                     8
                             11
    3
             6
                     9
                             12
```

List: Can store any type of objects together.

list1 = vector("list", 2)
list1[[1]] = v
list1[[2]] = M
list1[[3]] = arr
is.list(list1)
[1] TRUE
length(list1)
[1] 3
list1[[1]]
[1] 4 1 3

Important Functions

```
For Loop: To do a task many times. Simple, but inefficient
#First, create a large matrix
x <- matrix(rnorm(400*4000), ncol=400)
#Second, create a vector to store results
mx <- rep(NA, nrow(x))
#Third, for each row of the matrix, find the maximum value and store it in mx using
#a loop. We will do this from index 1 to the max number of rows (nrow(x)). We will
#iterate using index i.
for(i in 1:nrow(x)){
    mx[i] <- max(x[i,])
}</pre>
```

Apply: To do a task many times using vectorization. Much faster then a for loop.

The 1 indicates to the function 'max' on the rows of the object 'x'. A 2 would #that this function should be applied to each column of the object 'x'. $mx2 \leq apply(x, 1, max)$